CSCI 210: Computer Architecture Lecture 15: Digital Logic

Stephen Checkoway Oberlin College Nov. 5, 2021 Slides from Cynthia Taylor

Announcements

• Problem Set 4 due today

• Lab 3 due Sunday!

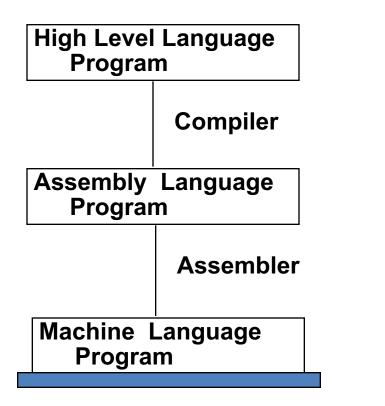
• Office Hours today 13:30 – 14:30 pm

Creating the Universe from 1 and 0

• We have seen how to build programs from assembly

 Now we'll learn how we build assembly language instructions out of circuits

Machine Interpretation



Machine Interpretation

temp = v[k]; v[k] = v[k+1]; v[k+1] = temp;

lw \$15, 0(\$2) lw \$16, 4(\$2) sw \$16, 0(\$2) sw \$15, 4(\$2)

Machine does something!

A digital circuit is comprised of signals, gates, and wires.

• Signals

-Voltages applied to lines which generate electric current

- Binary signals are represented by different voltages:
 - -0: 0-1 volts
 - -1: 2-5 volts

A digital circuit is comprised of signals, gates, and wires.

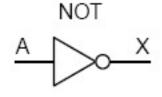
- Gates
 - Devices which perform operations on signals corresponding to basic logic operations: and, or, not, nand, nor, xor
 - -Made out of transistors

• Wires

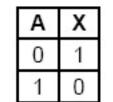
- Lines over which signals are transmitted between gates

Representation of Logic Gates

• Symbol



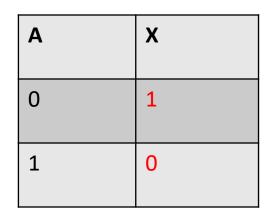
• Truth Table



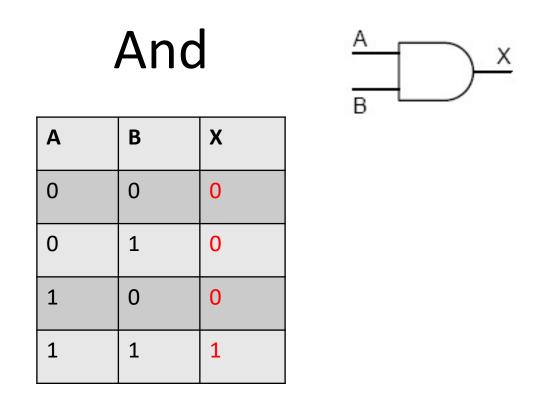
Ā

• Algebraic Representation



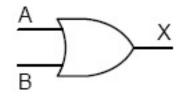


- Inverts the input
- Algebraic representation: \bar{A}



• Algebraic representation: AB or $A \cdot B$

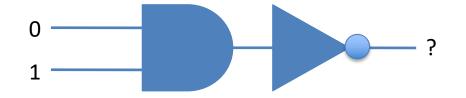




Α	В	x
0	0	0
0	1	1
1	0	1
1	1	1

• Algebraic representation: A+B

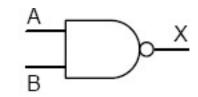
And and Not



A. 0

B. 1

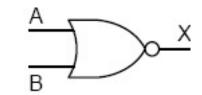




Α	В	Х
0	0	1
0	1	1
1	0	1
1	1	0

• Algebraic representation: $\overline{(A \cdot B)}$





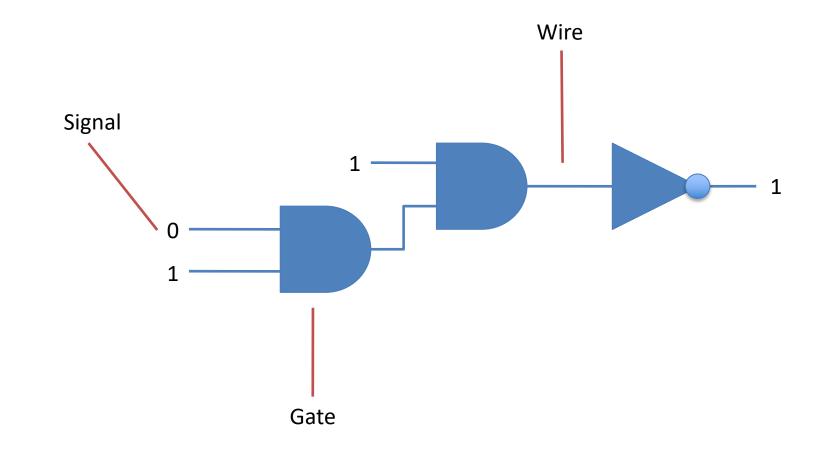
Α	В	x
0	0	1
0	1	0
1	0	0
1	1	0

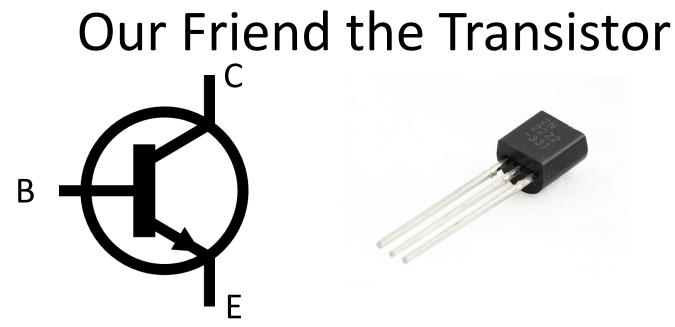
• Algebraic representation: $\overline{(A+B)}$



Α	В	x
0	0	0
0	1	1
1	0	1
1	1	0

- Algebraic representation: A^B or $A \oplus B$

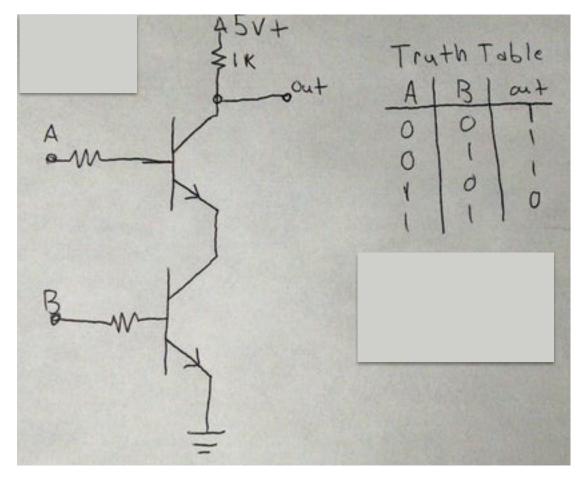




- The basic electronic component from which all gates are created; there are many types, this is an NPN transistor
- When the base (B) has a high voltage, current can flow from the collector (C) to the emitter (E)
- This creates an on/off switch

Building gates out of switches

- Two inputs A and B
- One output out
- When A or B are 1, the other two electrodes (collector and emitter) are connected
- When A and B are both 1, out is connected to ground (logic value 0)
- When either A or B is 0, out is not connected to ground and current can flow from 5V to out

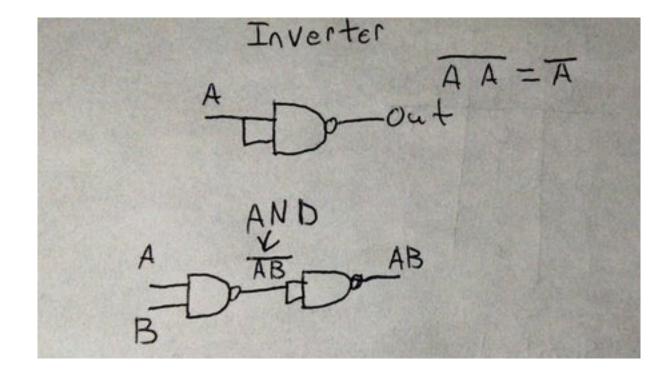


What Gate Does This Match?

- If A and B are high voltage (logical 1), C will be low voltage (logical 0)
- Otherwise, C is high voltage

- A. AND
- B. OR
- C. NAND
- D. NOR

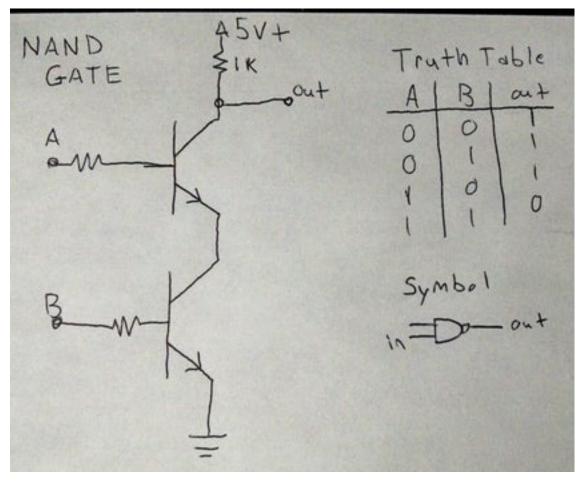
All Other Gates Can Be Created From NAND

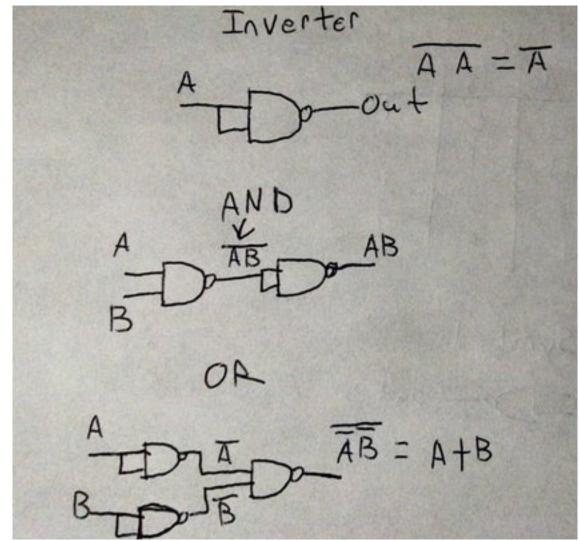


Which is equivalent to A OR B?

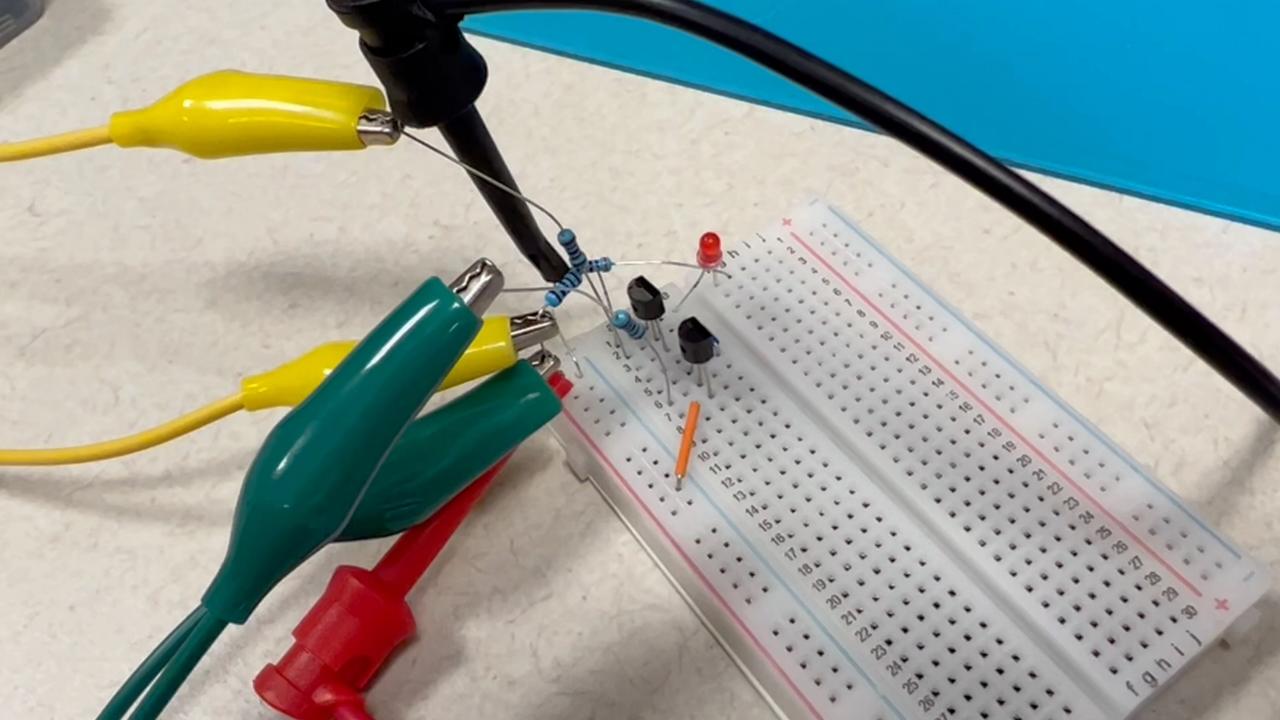
- A. A NAND B
- B. NOT (A NAND B)
- C. (NOT A) NAND (NOT B)
- D. NOT ((NOT A) NAND (NOT B))
- E. None of the above

Putting them together





Images from: https://www.instructables.com/Build-a-NAND-gate-from-transistors/



All Other Gates Can Be Created from NOR

• You will show this in Problem Set 5

Which column completes the truth table for

$$F = \overline{X} \cdot (Y + Z)?$$

- X Y Z A B C D
- 0 0 0 0 0 1 1
- 0 0 1 1 1 1 1
- 0 1 0 1 1 1 1
- 0 1 1 1 1 1 1
- 1 0 0 0 0 0
- 1 0 1 0 1 0 1
 - 1 1 0 0 1 0 1
 - 1 1 1 0 1 0 1

Diagram: $F = \overline{X} \cdot (Y + Z)$

 $F = \overline{A} + (B(AC + \overline{AB}))$

Truth Table

A B C AC \overline{AB} $B(AC + \overline{AB})$ F000 0 0 1 0 1 0 0 1 1 1 0 0 1 0 1 1 1 0 1 1 1

Reading

• Next lecture: Boolean Algebra

- 3.3

• Problem Set 4 due today

• Lab 3 due Sunday